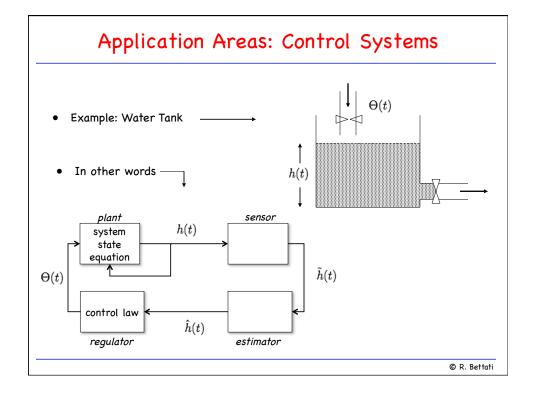
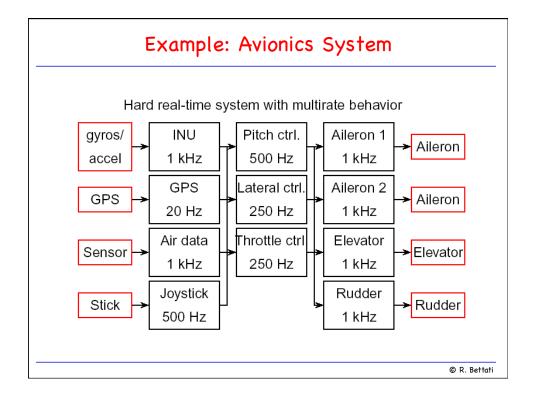
Real-Time Systems: Examples / Case Studies

- Simple Control System
- Sampling Periods
- · Quality of the Control vs. Processing Cost
- Protection of Resources in Integrated Systems
- Multimedia / Real-Time Communication
- Anomalies in Asynchronous Systems
 - Example: Advanced Fighter Technology Integration (AFTI) F16
- Priority Inversion
- Real-Time Systems
- Hard and soft deadlines; operational definition



Control Systems (cont)

• Control Loop:



Quality of Control vs. Processing Cost Example: Open-Loop Temperature Control

[Simplified from : Setol, Lehoczky, Sha, and Shin, "On Task Schedulability in Real-Time Control Systems", Proceeding of the 1996 IEEE Real-Time Systems Symposium]

System: Temperature of a unit is controlled by a burner.



Dynamic equation:

$$\dot{x} = -ax + bu$$

x - difference between unit and ambient temperature, x(0) = 0u - control input (rate of heat)

Control Problem: change temperature of unit to x_d within time $t_{\hat{p}\hat{i}}$ consume minimum amount of fuel. Allow for a tolerance δ .

$$|x(t_f) - x_d| \le \delta$$

Performance Index J(u) of control system: measure of total cost of control and accuracy generated in time period $[0, t_f]$ by control u. Generally: f^{t_f}

 $\overline{J(u)} = S(s(t_f), \overline{t_f}) + \int_0^{t_f} L(x(t), u(t), t) dt$

Optimal control $u^*(t)$ with performance index J^* .

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Open-Loop Temperature Control (cont)

Our case: minimize fuel.

$$min_u J = rac{1}{2} p(x(t_f) - x_d)^2 + rac{1}{2} \int_0^{t_f} u^2(t) dt$$

Resulting optimal control:

$$u^*(t) = rac{x_d pabe^{at}}{ae^{at_f} + pb^2 sinh(at_f)}$$

Final State:

$$x^*(t_f) = \frac{x_d p b^2 sinh(at_f)}{a e^{at_f} + p b^2 sinh(at_f)}$$

Open-Loop Temperature Control (cont)

Discretize control input u: Sampling period P.

$$\dot{x}^*(t) = -ax^*(t) + bu^*(kP)$$
 $kP \le t \le (k+1)P$

Performance index for discrete optimal control:

$$J_D^*(P) = S(x^*(t_f), t_f) + \sum_{k=0}^{n-1} \int_{kP}^{(k+1)P} L(x^*(t), u^*(kP), t) dt$$

In our case:

$$J_D^*(P) \tilde{=} \frac{1}{2} p x_d \left(\frac{1 - e^{-aP}}{1 + e^{-aP}} \right)$$

Constraints:

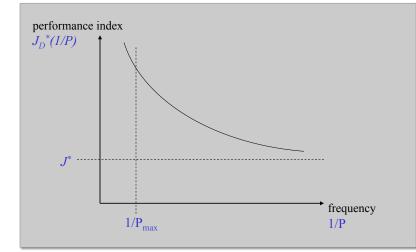
$$|x(t_f) - x_d| \le \delta$$

$$x_d \left(\frac{1 - e^{-aP}}{1 + e^{-aP}} \right) \le \delta \quad \Rightarrow \quad P \le \frac{1}{a} ln \frac{x_d + \delta}{x_d - \delta}$$

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Open-Loop Temperature Control (cont)

• Effect of sampling period on performance index.



Quality of Control vs. Processing Cost (cont)

Task frequencies must be determined to optimize the performance indices without overloading the available processing capabilities.

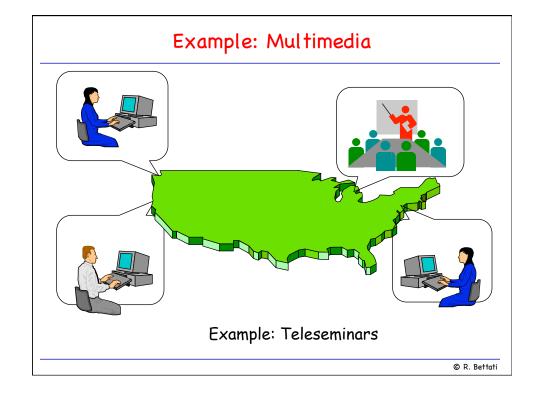
> $\Delta J^*(P) := J_D^*(P) - J^*$ Notation:

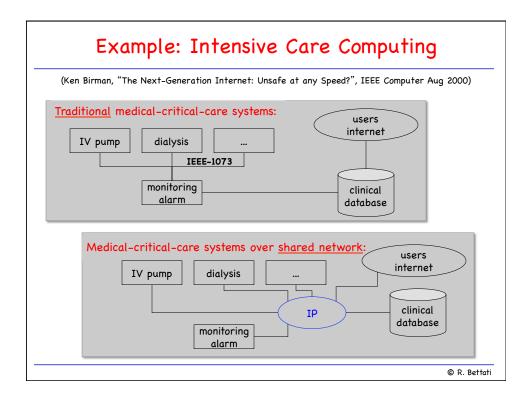
Optimization problem:

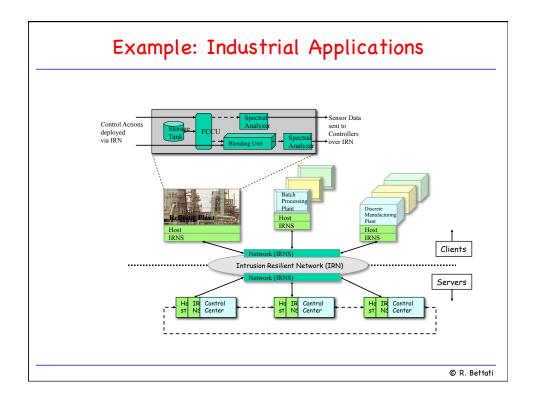
Given a set of tasks, T_{ν} ..., T_{n} , with given $\Delta \mathcal{J}_{i}^{*}(\bullet)$ and execution times C_{ν} , find a set of periods P_{i} , such that

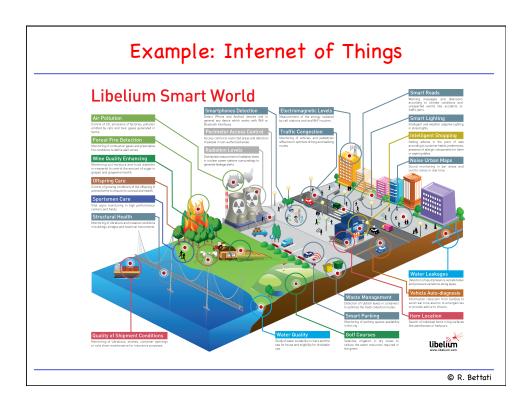
1. $P_i \leftarrow P_i^{max}$

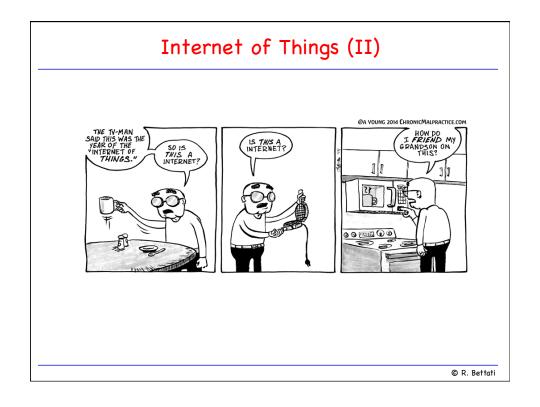
- // Maintain stability
- 2. Minimize (maximize) $\sum_{i=1}^n \Delta J_i^*(P_i)$ // Optimize total // performance index
- 3. Resource Constraint: $\sum_{i=1}^{n} \frac{1}{P_i} C_i \leq U$ // CPU capacity

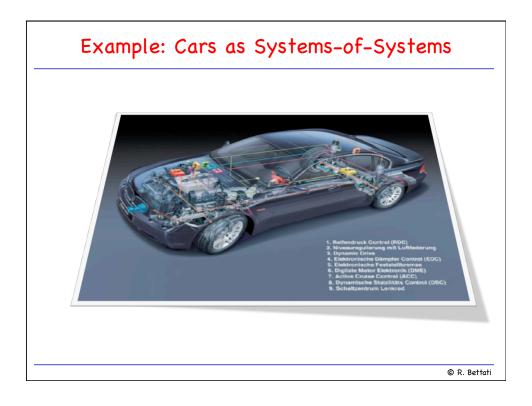


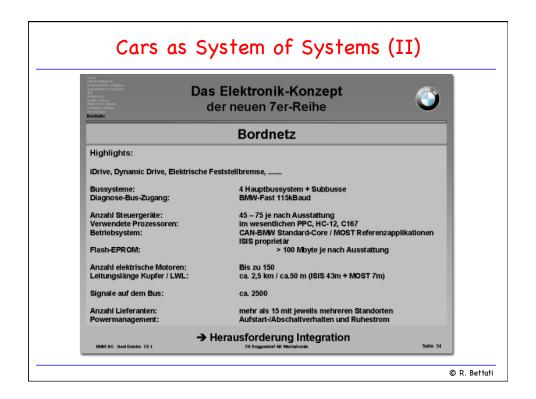


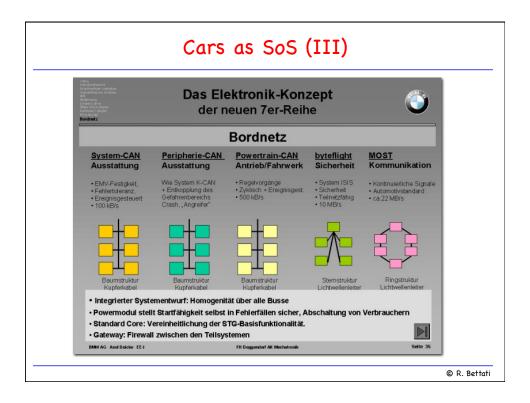


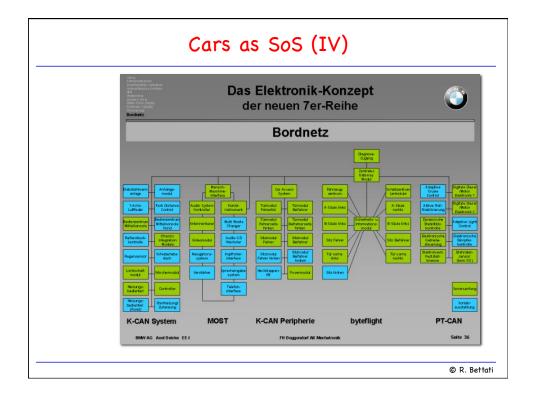


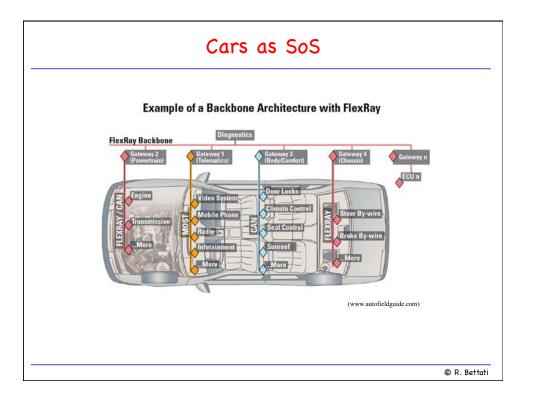


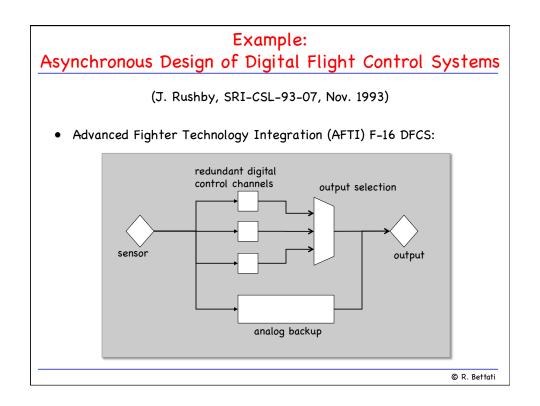












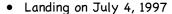
Asynchronous Design of Digital Flight Control Systems

'... The asynchronous design of the [AFTI-F16] DFCS introduced a random, unpredictable characteristic into the system. The system became untestable in that testing for each of the possible time relationships between the computers was impossible. This random time relationship was a major contributor to the flight test anomalies. Adversely affecting testability and having only postulated benefits, asynchronous operation of the DFCS demonstrated the need to avoid random, unpredictable, and uncompensated design characteristics.'

D. Mackall, flight-test engineer AFTI-F16 flight tests

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Example: Mars Pathfinder Incident

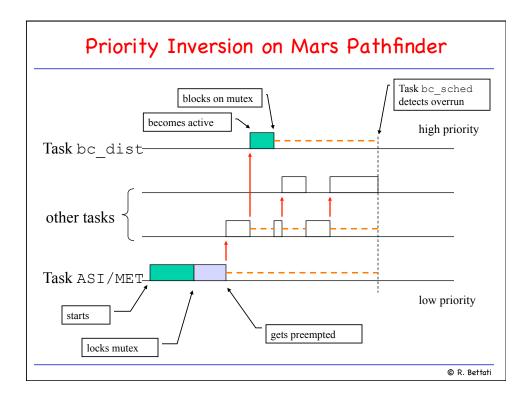


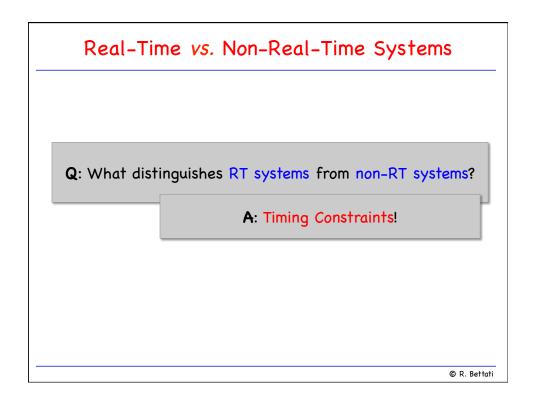
- "experiences software glitches"
- Pathfinder experiences repeated RESETs after starting gathering of meteorological data.
- RESETs generated by watchdog process.
- Timing overruns caused by priority inversion.

• Resources:

http://research.microsoft.com/enus/um/people/mbj/Mars_Pathfinder/ Mars Pathfinder.html







Players in Real-Time Systems

Jobs and Processors:

- Job: Unit of work executed by the system
- Processor: Jobs require resource to execute (CPU, disk, network link)

(We don't distinguish between types of processors!)

Timing constraints:

- Release Time: time when job becomes available for execution
- Deadline: time when execution must be completed
- Relative Deadline: maximum response time

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Hard vs. Soft Deadlines

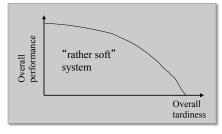
Hard Deadline: Late result may be a fatal flaw, of little use,

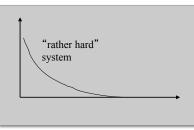
or cause disastrous consequences

Soft Deadline: Timely completion desirable.

Late results useful to some degree.

 Quantitative measure: Overall system performance as function of tardiness of jobs.





Operational Definition: A job has a hard deadline whenever the system designer must prove that the job never misses its deadline.

Hard Real-Time **Systems**

Definition: A real-time system is hard-realtime when a large portion of the deadlines is hard.

- Examples:
 - Embedded systems
 - Recovery procedures in high-availability systems
 - many others ...

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Hard Real-Time Systems

Q: Does real-time mean fast?

Q: Why not use commercial (general purpose) OSs? A: Verification, Certification

