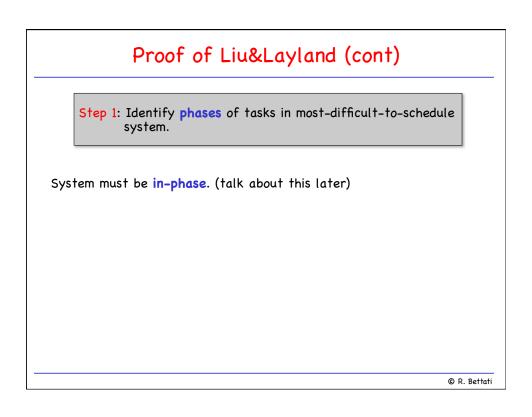
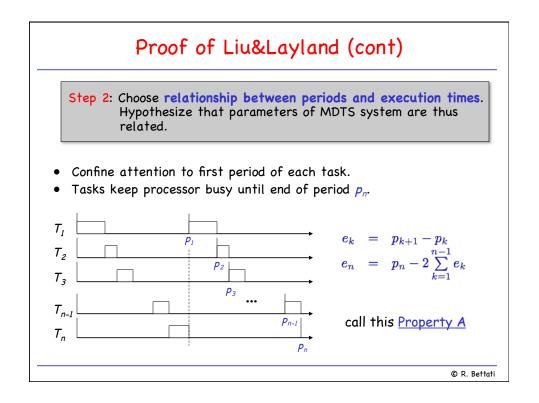
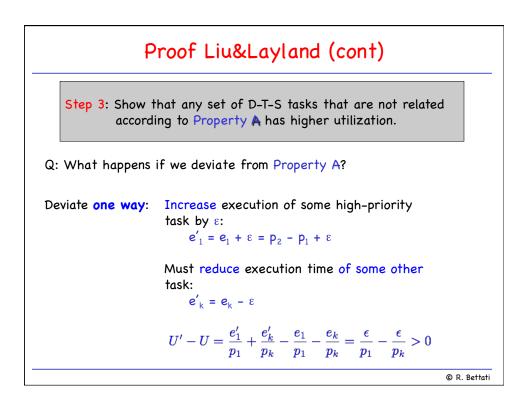
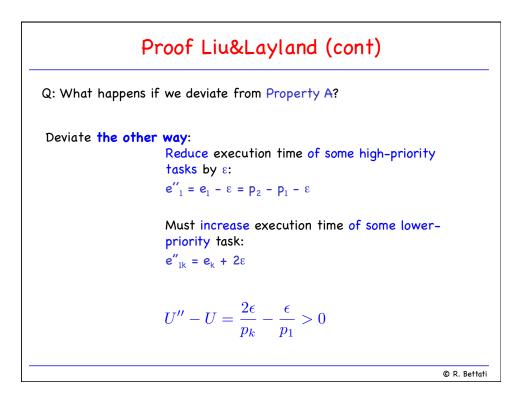


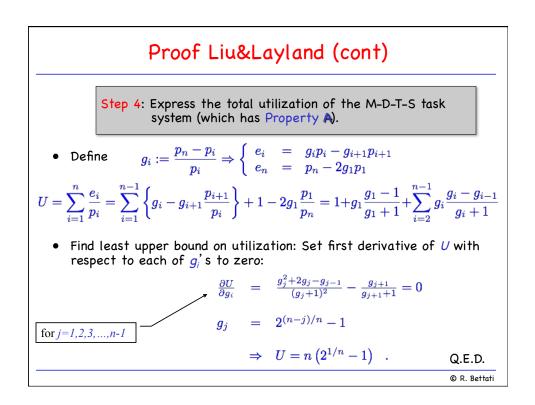
Proof of Liu&Layland		
• General idea:	Find the most-difficult-to-schedule system of <i>n</i> tasks among all difficult-to-schedule systems of <i>n</i> tasks.	
• Difficult-to-se	chedule : Fully utilizes processor for some time interval. Any increase in execution time would make system unschedulable.	
Most-difficult	- to-schedule : system with lowest utilization among difficult-to-schedule systems.	
• Each of the fo	llowing <u>4 steps</u> brings us closer to this system.	
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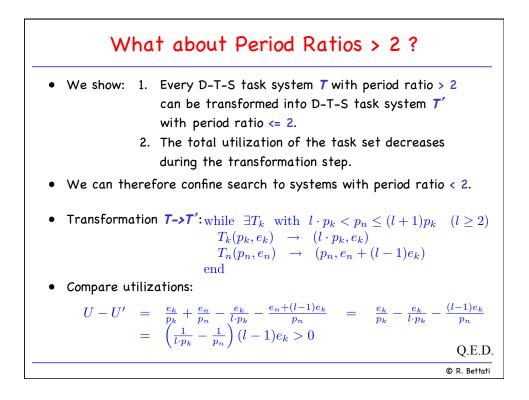


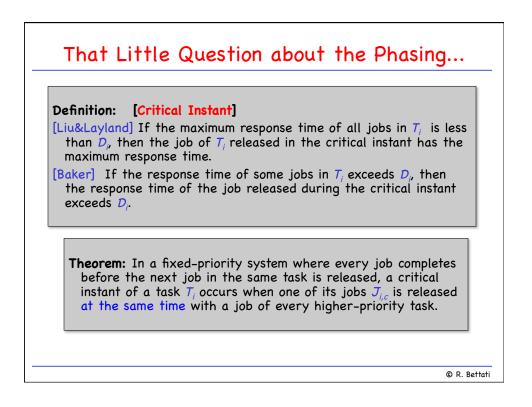












Proof (informal)	
• Assume:	Theorem holds for k < i.
• WLOG:	$\forall k < i : \varphi_k = 0$, and we look at $\mathcal{J}_{i,i}$
• Observation:	The completion time of higher-priority jobs is independent of the release time of $\mathcal{J}_{i,i}$.
• Therefore: The sooner $\mathcal{J}_{i,i}$ is released, the longer it has to wait until it is completed.	
	Q.E.D.
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